

## Multi-Step Equations

**Solve each equation.**

1)  $6a + 5a = -11$

2)  $-6n - 2n = 16$

3)  $4x + 6 + 3 = 17$

4)  $0 = -5n - 2n$

5)  $6r - 1 + 6r = 11$

6)  $r + 11 + 8r = 29$

7)  $-10 = -14v + 14v$

8)  $-10p + 9p = 12$

9)  $42 = 8m + 13m$

10)  $a - 2 + 3 = -2$

11)  $18 = 3(3x - 6)$

12)  $30 = -5(6n + 6)$

$$13) 37 = -3 + 5(x + 6)$$

$$14) -13 = 5(1 + 4m) - 2m$$

$$15) 4(-x + 4) = 12$$

$$16) -2 = -(n - 8)$$

$$17) -6(1 - 5v) = 54$$

$$18) 8 = 8v - 4(v + 8)$$

$$19) 10(1 + 3b) = -20$$

$$20) -5n - 8(1 + 7n) = -8$$

$$21) 8(4k - 4) = -5k - 32$$

$$22) -8(-8x - 6) = -6x - 22$$

$$23) 8(1 + 5x) + 5 = 13 + 5x$$

$$24) -11 - 5a = 6(5a + 4)$$

$$25) -5(4x - 2) = -2(3 + 6x)$$

$$26) 5(2x + 6) = -4(-5 - 2x) + 3x$$

## Multi-Step Equations

**Solve each equation.**

1)  $6a + 5a = -11$

 $\{-1\}$ 

2)  $-6n - 2n = 16$

 $\{-2\}$ 

3)  $4x + 6 + 3 = 17$

 $\{2\}$ 

4)  $0 = -5n - 2n$

 $\{0\}$ 

5)  $6r - 1 + 6r = 11$

 $\{1\}$ 

6)  $r + 11 + 8r = 29$

 $\{2\}$ 

7)  $-10 = -14v + 14v$

No solution.

8)  $-10p + 9p = 12$

 $\{-12\}$ 

9)  $42 = 8m + 13m$

 $\{2\}$ 

10)  $a - 2 + 3 = -2$

 $\{-3\}$ 

11)  $18 = 3(3x - 6)$

 $\{4\}$ 

12)  $30 = -5(6n + 6)$

 $\{-2\}$

$$13) 37 = -3 + 5(x + 6)$$

{2}

$$14) -13 = 5(1 + 4m) - 2m$$

{-1}

$$15) 4(-x + 4) = 12$$

{1}

$$16) -2 = -(n - 8)$$

{10}

$$17) -6(1 - 5v) = 54$$

{2}

$$18) 8 = 8v - 4(v + 8)$$

{10}

$$19) 10(1 + 3b) = -20$$

{-1}

$$20) -5n - 8(1 + 7n) = -8$$

{0}

$$21) 8(4k - 4) = -5k - 32$$

{0}

$$22) -8(-8x - 6) = -6x - 22$$

{-1}

$$23) 8(1 + 5x) + 5 = 13 + 5x$$

{0}

$$24) -11 - 5a = 6(5a + 4)$$

{-1}

$$25) -5(4x - 2) = -2(3 + 6x)$$

{2}

$$26) 5(2x + 6) = -4(-5 - 2x) + 3x$$

{10}

1. Add or subtract the following polynomials and simplify.

(a)  $(5x + 2) + (3x + 6)$

(b)  $(9x - 8) - (2x + 1)$

(c)  $(-7x^2 + x + 2) - (9x^2 + 6)$

(d)  $(2x + 1) + (6x + 1)$

(e)  $(6y + 4) + (2y + 12)$

(f)  $(z - 16) + 7(3z + 6) - (2z + 1)$

(g)  $(6z^2 + 2) + z(2z + 4) - 2(2z + 6)$

(h)  $(7x^3 + 3x^2 - 2) + x^2(3x + 6)$

(i)  $x(x^2 + 2) - 2x^2(3x + 6)$

(j)  $(-12x^4 + 18x^2) + 3x^2(4x^2 - 6)$

2. Multiply and simplify the following expressions.

(a)  $(x + 4)(x^2 - 2x + 5)$

(b)  $(2x^3 - 8)(4x^2 + x)$

(c)  $(\sqrt{x} + 2)(\sqrt{x} + 6)$

(d)  $(\sqrt{x} + 1)(\sqrt{x} - 1)$

(e)  $\sqrt{x}(x + \sqrt{x})$

(f)  $z^{1/4}(z^{1/2} + z^{3/4})$

(g)  $((6z^2 + 2) + z^2)((6z^2 + 2) - z^2)$

(h)  $(\sqrt{x^2 - 3} + 3)(\sqrt{x^2 - 3} - 3)$

(i)  $(x^{1/2} + y^2)(x^{1/2} - y^2)$

(j)  $(2x + 3)(2x - 3)$

(k)  $(5x - \sqrt{3})(5x + \sqrt{3})$

(l)  $(2x^2 - y^2)(2x^2 + y^2)$

3. Expand the following.

(a)  $(2b + 1)^2$

(b)  $(3 + x)^4$

(c)  $(1 - 3m)^3$

(d)  $(y + 2)^3$

(e)  $(y - 4)^4$

(f)  $(4y - 1)^3$

(g)  $(2x - 3)^3$

(h)  $(x - 2)^5$

(i)  $(2x + 1)^4$

4. Divide.

(a)  $(12x^3 - 11x^2 + 9x + 18) \div (4x + 3)$

(b)  $(2x^4 - x^3 - 7x^2 - 3x + 10) \div (x - 2)$

(c)  $(5x^3 - x^2 + 6) \div (x + 1)$

(d)  $(x^4 + 4x^3 + x - 10) \div (x^2 + 3x - 5)$

(e)  $(6x^3 - 8x + 5) \div (2x - 4)$

(f)  $(x^3 - 4x^2 + 2x - 5) \div (x - 2)$

(g)  $(2x^3 + 4x^2 - 5) \div (x + 3)$

(h)  $(2x^3 - 4x + 7x^2 + 7) \div (x^2 + 2x - 1)$

(i)  $(4x^3 - 2x^2 - 3) \div (2x^2 - 1)$

(j)  $(3x^3 + 4x + 11) \div (x^2 - 3x + 2)$

5. Divide the following polynomials.

(a)  $(4b^3 - 16b^2 - 2) \div (b - 4)$

(b)  $(a^3 + 12a^2 + 34a - 19) \div (a + 6)$

(c)  $(7k^3 - 42k^2 - 9) \div (k - 6)$

(d)  $(p^3 - 36p - 10) \div (p - 6)$

(e)  $(5p^3 - 32p^2 + 44p - 45) \div (p - 5)$

(f)  $\frac{x^3 + 9x^2 + 17x - 12}{x + 4}$



# Answers

1. (a)  $8x + 8$  (b)  $7x - 9$  (c)  $-16x^2 + x - 8$  (d)  $8x + 2$   
(e)  $8y + 16$  (f)  $20z + 25$  (g)  $8z^2 - 10$  (h)  $10x^3 + 9x^2 - 2$   
(i)  $-5x^3 - 12x^2 + 2x$  (j)  $0$
2. (a)  $x^3 + 2x^2 - 3x + 20$  (b)  $8x^5 + 2x^4 - 32x^2 - 8x$  (c)  $x + 8\sqrt{x} + 12$   
(d)  $x - 1$  (e)  $x^{3/2} + x$  (f)  $z^{3/4} + z$   
(g)  $35z^4 + 24z^2 + 4$  (h)  $x^2 - 12$  (i)  $x - y^4$   
(j)  $4x^2 - 9$  (k)  $25x^2 - 3$  (l)  $4x^4 - y^4$
3. (a)  $4b^2 + 4b + 1$  (b)  $81 + 108x + 54x^2 + 12x^3 + x^4$   
(c)  $1 - 9m + 27m^2 - 27m^3$  (d)  $y^3 + 6y^2 + 12y + 8$   
(e)  $y^4 - 16y^3 + 96y^2 - 256y + 256$  (f)  $64y^3 - 48y^2 + 12y - 1$   
(g)  $8x^3 - 36x^2 + 54x - 27$  (h)  $x^5 - 10x^4 + 40x^3 - 80x^2 + 80x - 32$   
(i)  $16x^4 + 32x^3 + 24x^2 + 8x + 1$
4. (a)  $3x^2 - 5x + 6$  (b)  $2x^3 + 3x^2 - x - 5$  (c)  $5x^2 - 6x + 6$   
(d)  $x^2 + x + 2$  (e)  $3x^2 + 6x + 8 + \frac{37}{2(x-2)}$  (f)  $x^2 - 2x - 2 - \frac{9}{x-2}$   
(g)  $2x^2 - 2x + 6 - \frac{23}{x+3}$  (h)  $2x + 3 - \frac{2(4x-5)}{x^2+2x-1}$  (i)  $2x - 1 + \frac{2(x-2)}{2x^2-1}$   
(j)  $3x + 9 + \frac{25x-7}{x^2-3x+2}$
5. (a)  $4b^2 - \frac{2}{b-4}$  (b)  $a^2 + 6a - 2 - \frac{7}{a+6}$  (c)  $7k^2 - \frac{9}{k-6}$   
(d)  $p^2 + 6p - \frac{10}{p-6}$  (e)  $5p^2 - 7p + 9$  (f)  $x^2 + 5x - 3$

## Factoring Trinomials (a = 1)

**Factor each completely.**

1)  $b^2 + 8b + 7$

2)  $n^2 - 11n + 10$

3)  $m^2 + m - 90$

4)  $n^2 + 4n - 12$

5)  $n^2 - 10n + 9$

6)  $b^2 + 16b + 64$

7)  $m^2 + 2m - 24$

8)  $x^2 - 4x + 24$

9)  $k^2 - 13k + 40$

10)  $a^2 + 11a + 18$

11)  $n^2 - n - 56$

12)  $n^2 - 5n + 6$

13)  $b^2 - 6b + 8$

14)  $n^2 + 6n + 8$

15)  $2n^2 + 6n - 108$

16)  $5n^2 + 10n + 20$

17)  $2k^2 + 22k + 60$

18)  $a^2 - a - 90$

19)  $p^2 + 11p + 10$

20)  $5v^2 - 30v + 40$

21)  $2p^2 + 2p - 4$

22)  $4v^2 - 4v - 8$

23)  $x^2 - 15x + 50$

24)  $v^2 - 7v + 10$

25)  $p^2 + 3p - 18$

26)  $6v^2 + 66v + 60$

## Factoring Trinomials (a = 1)

**Factor each completely.**

1)  $b^2 + 8b + 7$

$(b + 7)(b + 1)$

2)  $n^2 - 11n + 10$

$(n - 10)(n - 1)$

3)  $m^2 + m - 90$

$(m - 9)(m + 10)$

4)  $n^2 + 4n - 12$

$(n - 2)(n + 6)$

5)  $n^2 - 10n + 9$

$(n - 1)(n - 9)$

6)  $b^2 + 16b + 64$

$(b + 8)^2$

7)  $m^2 + 2m - 24$

$(m + 6)(m - 4)$

8)  $x^2 - 4x + 24$

Not factorable

9)  $k^2 - 13k + 40$

$(k - 5)(k - 8)$

10)  $a^2 + 11a + 18$

$(a + 2)(a + 9)$

11)  $n^2 - n - 56$

$(n + 7)(n - 8)$

12)  $n^2 - 5n + 6$

$(n - 2)(n - 3)$

13)  $b^2 - 6b + 8$

$(b - 4)(b - 2)$

14)  $n^2 + 6n + 8$

$(n + 2)(n + 4)$

15)  $2n^2 + 6n - 108$

$2(n + 9)(n - 6)$

16)  $5n^2 + 10n + 20$

$5(n^2 + 2n + 4)$

17)  $2k^2 + 22k + 60$

$2(k + 5)(k + 6)$

18)  $a^2 - a - 90$

$(a - 10)(a + 9)$

19)  $p^2 + 11p + 10$

$(p + 10)(p + 1)$

20)  $5v^2 - 30v + 40$

$5(v - 2)(v - 4)$

21)  $2p^2 + 2p - 4$

$2(p - 1)(p + 2)$

22)  $4v^2 - 4v - 8$

$4(v + 1)(v - 2)$

23)  $x^2 - 15x + 50$

$(x - 10)(x - 5)$

24)  $v^2 - 7v + 10$

$(v - 5)(v - 2)$

25)  $p^2 + 3p - 18$

$(p - 3)(p + 6)$

26)  $6v^2 + 66v + 60$

$6(v + 10)(v + 1)$

## Solving Quadratic Equations by Factoring

Solve each equation by factoring.

1)  $(k + 1)(k - 5) = 0$

2)  $(a + 1)(a + 2) = 0$

3)  $(4k + 5)(k + 1) = 0$

4)  $(2m + 3)(4m + 3) = 0$

5)  $x^2 - 11x + 19 = -5$

6)  $n^2 + 7n + 15 = 5$

7)  $n^2 - 10n + 22 = -2$

8)  $n^2 + 3n - 12 = 6$

9)  $6n^2 - 18n - 18 = 6$

10)  $7r^2 - 14r = -7$

$$11) n^2 + 8n = -15$$

$$12) 5r^2 - 44r + 120 = -30 + 11r$$

$$13) -4k^2 - 8k - 3 = -3 - 5k^2$$

$$14) b^2 + 5b - 35 = 3b$$

$$15) 3r^2 - 16r - 7 = 5$$

$$16) 6b^2 - 13b + 3 = -3$$

$$17) 7k^2 - 6k + 3 = 3$$

$$18) 35k^2 - 22k + 7 = 4$$

$$19) 7x^2 + 2x = 0$$

$$20) 10b^2 = 27b - 18$$

$$21) 8x^2 + 21 = -59x$$

$$22) 15a^2 - 3a = 3 - 7a$$

## Solving Quadratic Equations by Factoring

**Solve each equation by factoring.**

1)  $(k + 1)(k - 5) = 0$

$\{-1, 5\}$

2)  $(a + 1)(a + 2) = 0$

$\{-1, -2\}$

3)  $(4k + 5)(k + 1) = 0$

$\left\{-\frac{5}{4}, -1\right\}$

4)  $(2m + 3)(4m + 3) = 0$

$\left\{-\frac{3}{2}, -\frac{3}{4}\right\}$

5)  $x^2 - 11x + 19 = -5$

$\{3, 8\}$

6)  $n^2 + 7n + 15 = 5$

$\{-5, -2\}$

7)  $n^2 - 10n + 22 = -2$

$\{6, 4\}$

8)  $n^2 + 3n - 12 = 6$

$\{3, -6\}$

9)  $6n^2 - 18n - 18 = 6$

$\{4, -1\}$

10)  $7r^2 - 14r = -7$

$\{1\}$



11)  $n^2 + 8n = -15$

$\{-5, -3\}$

12)  $5r^2 - 44r + 120 = -30 + 11r$

$\{6, 5\}$

13)  $-4k^2 - 8k - 3 = -3 - 5k^2$

$\{8, 0\}$

14)  $b^2 + 5b - 35 = 3b$

$\{-7, 5\}$

15)  $3r^2 - 16r - 7 = 5$

$\left\{-\frac{2}{3}, 6\right\}$

16)  $6b^2 - 13b + 3 = -3$

$\left\{\frac{2}{3}, \frac{3}{2}\right\}$

17)  $7k^2 - 6k + 3 = 3$

$\left\{\frac{6}{7}, 0\right\}$

18)  $35k^2 - 22k + 7 = 4$

$\left\{\frac{1}{5}, \frac{3}{7}\right\}$

19)  $7x^2 + 2x = 0$

$\left\{-\frac{2}{7}, 0\right\}$

20)  $10b^2 = 27b - 18$

$\left\{\frac{6}{5}, \frac{3}{2}\right\}$

21)  $8x^2 + 21 = -59x$

$\left\{-\frac{3}{8}, -7\right\}$

22)  $15a^2 - 3a = 3 - 7a$   $\left\{\frac{1}{3}, -\frac{3}{5}\right\}$

## Using the Quadratic Formula

**Solve each equation with the quadratic formula.**

1)  $m^2 - 5m - 14 = 0$

2)  $b^2 - 4b + 4 = 0$

3)  $2m^2 + 2m - 12 = 0$

4)  $2x^2 - 3x - 5 = 0$

5)  $x^2 + 4x + 3 = 0$

6)  $2x^2 + 3x - 20 = 0$

7)  $4b^2 + 8b + 7 = 4$

8)  $2m^2 - 7m - 13 = -10$

$$9) 2x^2 - 3x - 15 = 5$$

$$10) x^2 + 2x - 1 = 2$$

$$11) 2k^2 + 9k = -7$$

$$12) 5r^2 = 80$$

$$13) 2x^2 - 36 = x$$

$$14) 5x^2 + 9x = -4$$

$$15) k^2 - 31 - 2k = -6 - 3k^2 - 2k$$

$$16) 9n^2 = 4 + 7n$$

$$17) 8n^2 + 4n - 16 = -n^2$$

$$18) 8n^2 + 7n - 15 = -7$$

## Using the Quadratic Formula

**Solve each equation with the quadratic formula.**

1)  $m^2 - 5m - 14 = 0$

$\{7, -2\}$

2)  $b^2 - 4b + 4 = 0$

$\{2\}$

3)  $2m^2 + 2m - 12 = 0$

$\{2, -3\}$

4)  $2x^2 - 3x - 5 = 0$

$\left\{\frac{5}{2}, -1\right\}$

5)  $x^2 + 4x + 3 = 0$

$\{-1, -3\}$

6)  $2x^2 + 3x - 20 = 0$

$\left\{\frac{5}{2}, -4\right\}$

7)  $4b^2 + 8b + 7 = 4$

$\left\{-\frac{1}{2}, -\frac{3}{2}\right\}$

8)  $2m^2 - 7m - 13 = -10$

$\left\{\frac{7 + \sqrt{73}}{4}, \frac{7 - \sqrt{73}}{4}\right\}$

9)  $2x^2 - 3x - 15 = 5$

$$\left\{4, -\frac{5}{2}\right\}$$

10)  $x^2 + 2x - 1 = 2$

$$\{1, -3\}$$

11)  $2k^2 + 9k = -7$

$$\left\{-1, -\frac{7}{2}\right\}$$

12)  $5r^2 = 80$

$$\{4, -4\}$$

13)  $2x^2 - 36 = x$

$$\left\{\frac{9}{2}, -4\right\}$$

14)  $5x^2 + 9x = -4$

$$\left\{-\frac{4}{5}, -1\right\}$$

15)  $k^2 - 31 - 2k = -6 - 3k^2 - 2k$

$$\left\{\frac{5}{2}, -\frac{5}{2}\right\}$$

16)  $9n^2 = 4 + 7n$

$$\left\{\frac{7 + \sqrt{193}}{18}, \frac{7 - \sqrt{193}}{18}\right\}$$

17)  $8n^2 + 4n - 16 = -n^2$

$$\left\{\frac{-2 + 2\sqrt{37}}{9}, \frac{-2 - 2\sqrt{37}}{9}\right\}$$

18)  $8n^2 + 7n - 15 = -7$

$$\left\{\frac{-7 + \sqrt{305}}{16}, \frac{-7 - \sqrt{305}}{16}\right\}$$