
NEAR-INFRARED SPECTROSCOPY IN FOOD SCIENCE AND TECHNOLOGY

Edited By

Yukihiro Ozaki, PhD

Kwansei Gakuin University
Japan

W. Fred McClure, PhD

North Carolina State University
Raleigh, North Carolina

Alfred A. Christy, PhD

Adger University
Kristiansand, Norway



WILEY-INTERSCIENCE

A John Wiley & Sons, Inc., Publication

**NEAR-INFRARED
SPECTROSCOPY IN
FOOD SCIENCE AND
TECHNOLOGY**



THE WILEY BICENTENNIAL—KNOWLEDGE FOR GENERATIONS

Each generation has its unique needs and aspirations. When Charles Wiley first opened his small printing shop in lower Manhattan in 1807, it was a generation of boundless potential searching for an identity. And we were there, helping to define a new American literary tradition. Over half a century later, in the midst of the Second Industrial Revolution, it was a generation focused on building the future. Once again, we were there, supplying the critical scientific, technical, and engineering knowledge that helped frame the world. Throughout the 20th Century, and into the new millennium, nations began to reach out beyond their own borders and a new international community was born. Wiley was there, expanding its operations around the world to enable a global exchange of ideas, opinions, and know-how.

For 200 years, Wiley has been an integral part of each generation's journey, enabling the flow of information and understanding necessary to meet their needs and fulfill their aspirations. Today, bold new technologies are changing the way we live and learn. Wiley will be there, providing you the must-have knowledge you need to imagine new worlds, new possibilities, and new opportunities.

Generations come and go, but you can always count on Wiley to provide you the knowledge you need, when and where you need it!

WILLIAM J. PESCE
PRESIDENT AND CHIEF EXECUTIVE OFFICER

PETER BOOTH WILEY
CHAIRMAN OF THE BOARD

NEAR-INFRARED SPECTROSCOPY IN FOOD SCIENCE AND TECHNOLOGY

Edited By

Yukihiro Ozaki, PhD

Kwansei Gakuin University
Japan

W. Fred McClure, PhD

North Carolina State University
Raleigh, North Carolina

Alfred A. Christy, PhD

Adger University
Kristiansand, Norway



WILEY-INTERSCIENCE

A John Wiley & Sons, Inc., Publication

Copyright © 2007 by John Wiley & Sons, Inc. All rights reserved

Published by John Wiley & Sons, Inc., Hoboken, New Jersey
Published simultaneously in Canada

No part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanical, photocopying, recording, scanning, or otherwise, except as permitted under Section 107 or 108 of the 1976 United States Copyright Act, without either the prior written permission of the Publisher, or authorization through payment of the appropriate per-copy fee to the Copyright Clearance Center, Inc., 222 Rosewood Drive, Danvers, MA 01923, (978) 750-8400, fax (978) 750-4470, or on the web at www.copyright.com. Requests to the Publisher for permission should be addressed to the Permissions Department, John Wiley & Sons, Inc., 111 River Street, Hoboken, NJ 07030, (201) 748-6011, fax (201) 748-6008, or online at <http://www.wiley.com/go/permission>.

Limit of Liability/Disclaimer of Warranty: While the publisher and author have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. No warranty may be created or extended by sales representatives or written sales materials. The advice and strategies contained herein may not be suitable for your situation. You should consult with a professional where appropriate. Neither the publisher nor author shall be liable for any loss of profit or any other commercial damages, including but not limited to special, incidental, consequential, or other damages.

For general information on our other products and services or for technical support, please contact our Customer Care Department within the United States at (800) 762-2974, outside the United States at (317) 572-3993 or fax (317) 572-4002.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic formats. For more information about Wiley products, visit our web site at www.wiley.com.

Library of Congress Cataloging-in-Publication Data:

Near-infrared spectroscopy in food science and technology / edited by

Yukihiro Ozaki, W. Fred McClure, Alfred Christy.

p. cm.

Includes bibliographical references and index.

ISBN-13: 978-0-471-67201-2 (acid-free paper)

ISBN-10: 0-471-67201-7 (acid-free paper)

1. Food—Analysis. 2. Near infrared spectroscopy. I. Ozaki, Y. (Yukihiro)
II. McClure, W. F. (William F.) III. Christy, Alfred A.

TX547.2.I53N426 2006

664'.07—dc22

2006040965

Printed in the United States of America

10 9 8 7 6 5 4 3 2 1

CONTENTS

1. Introduction	1
<i>W. Fred McClure</i>	
2. Principles of Molecular Vibrations for Near-Infrared Spectroscopy	11
<i>C. Sandorfy, R. Buchet, and G. Lachenal</i>	
3. Spectral Analysis	47
<i>Yukihiro Ozaki, Shigeaki Morita, and Yiping Du</i>	
CHAPTER 4 INSTRUMENTATION	73
4.1. Instruments	75
<i>W. F. McClure and Satoru Tsuchikawa</i>	
4.2. Time-of-Flight Spectroscopy	109
<i>Satoru Tsuchikawa and W. Fred McClure</i>	
4.3. NIR Imaging and its Applications to Agricultural and Food Engineering	121
<i>E. Neil Lewis, Janie Dubois, and Linda H. Kidder</i>	
5. Sampling Techniques	133
<i>Satoru Tsuchikawa</i>	
6. Latent-Variable Analysis of Multivariate Data in Infrared Spectrometry	145
<i>Alfred A. Christy and Olav M. Kvalheim</i>	
CHAPTER 7 APPLICATIONS TO AGRICULTURAL AND MARINE PRODUCTS	163
7.1. Grains and Seeds	165
<i>Phil Williams</i>	

7.2. Fruits and Vegetables	219
<i>Sirinnapa Saranwong and Sumio Kawano</i>	
7.3. Meat and Fish Products	247
<i>Tomas Isaksson and Vegard H. Segtnan</i>	
CHAPTER 8 APPLICATIONS TO FOODSTUFFS	279
8.1. Flours and Breads	281
<i>Brian G. Osborne</i>	
8.2. Cereal Foods	297
<i>Sandra E. Kays and Franklin E. Barton, II</i>	
8.3. Livestock Animal By-Products	311
<i>D. Cozzolino</i>	
8.4. Dairy Products	323
<i>R. Giangiacomo and T.M.P. Cattaneo</i>	
CHAPTER 9 OTHER TOPICS	341
9.1. Fermentation Engineering	343
<i>Takuo Yano</i>	
9.2. On-Line Analysis in Food Engineering	361
<i>Kathryn A. Lee</i>	
9.3. Disease Diagnosis Related to Food Safety in Dairy	379
<i>Roumiana Tsenkova</i>	
INDEX	401

PREFACE

Near-infrared (NIR) spectroscopy has recently become increasingly important in food science and technology as a non-destructive analytical technique. An enormous number of articles and research papers are published every year that deal with applications of NIR spectroscopy in this important field. Search for a comprehensive book describing both basic principles and modern application of NIR spectroscopy food science and technology proved fruitless. This book, *Near Infrared Spectroscopy in Food Science and Technology*, fills the void. It covers principles of molecular vibrations, spectral analysis, and instrumentation for NIR spectroscopy as well as its novel applications within food science and technology. It is written to be appreciated by food and agricultural scientists and engineers as well as molecular spectroscopists. The aim of this book is to provide a basic understanding of techniques and applications that demonstrate the potential of NIR spectroscopy for researchers and users in food science and technology.

The book is suitable for students at graduate level as well as researchers and engineers in academic and industry. It may be used as a textbook for a graduate course in food science and technology or agricultural science and technology and for short courses. We hope you enjoy this book and that it will inspire you and other readers to adapt the principles and techniques discussed herein to your particular area and interests.

Yukihiro Ozaki
W. Fred McClure
Alfred Christy

ACKNOWLEDGMENTS

The editors thank each contributor who took time from their normal duties to make this book possible. We especially thank Ms. K. Horiguchi for the preparation of manuscripts, figures, and references. We also would like to thank both families and colleagues who provided encouragement and other support – making the tasks joy rather than drudgery. We hope all our readers enjoy this book.

CONTRIBUTORS

- Franklin E. Barton II**, U. S. Department of Agriculture, Agricultural Research Service, Richard B. Russell Agricultural Center, P. O. Box 5677, Athens, GA 30613, USA
- Greame D. Batten**, Farrer Centre, Charles Sturt University, LMB Bag 588 Wagga Wagga, NSW 2678, Australia
- R. Buchet**, UFR Chimie Biochimie, Universite Claude Bernard Lyon I, 43 Boulevard 11 November 1918, 69622 Villeurbanne Cedex, France
- T.M.P. Cattaneo**, Istituto Sperimentale Lattiero Caseario, Via A. Lombardo, 11-26900 Lodi, Italy
- Alfred A. Christy**, Adger University, Faculty of Mathematics and Sciences, Torden-skjolds gate 65, N-4604 Kristiansand, Norway
- D. Cozzolino**, Australian Wine Institute in Glan Osmond, Adelaide, Australia
- Geraed Downey**, The National Food Centre, Research & Training for the Food Industry, Dunsinea, Castleknock, Dublin 15, Ireland
- Yiping Du**, Analysis and Research Center, East China University of Science and Technology, Meilong Road 130, Shenghai 200237, China
- Janie Dubois**, Joint Institute for Food Safety and Applied Nutrition, University of Maryland and U.S. Food and Drug Administration, HFS-717, 5100 Paint Branch Parkway, College Park, MD, USA
- R. Giangiacomo**, Istituto Sperimentale Lattiero Caseario, Via A. Lombardo, 11-26900 LODI, Italy
- Kjell Ivar Hildrum**, MATFORSK, Norwegian Food Research Institute, N-1430 As, Norway
- Tomas Isaksson**, Agricultural University of Norway, Department of Food Science, P. O. Box 5036, N-1432 As, Norway
- Sumio Kawano**, Nondestructive Evaluation Laboratory, Analytical Science Division, National Food Research Institute, 2-1-2, Kannondai, Tsukuba, 305-8642, Japan

Sandra E. Kays, U. S. Department of Agriculture, Agricultural Research Service, Quality Assessment Research Unit, 950 College Station Rd., Athens, GA 30605, USA

Linda H. Kidder, Spectral Dimensions, 3416 Olandwood Court, Olney, MD 20832, USA

Olav M. Kvalheim, University of Bergen, Department of Chemistry, Allegaten 41, N-5007 Bergen, Norway

G. Lachenal, UFR Chimie Biochimie, Universite Claude Bernard Lyon I, 43 Boulevard 11 November 1918, 69622 Villeurbanne Cedex, France

Kathryn A. Lee, 239 Spencer Road, Basking Ridge, NJ 07920, USA

E. Neil Lewis, Spectral Dimensions, 3403 Olandwood Ct, Suite 102, Olney, MD 20832, USA

W. Fred McClure, NC State University, Biological and Agricultural Engineering Department, Campus Box 7625, Raleigh, NC 27695-7625, USA

Shigeaki Morita, Department of Chemistry, School of Science and Technology, Kwansai-Gakuin University, 2-1, Gakuen, Sanda, 669-1337, Japan

Ian Murray, Scottish Agricultural College, Craibstone, Aberdeen, AB21 9YA, UK

Brian G. Osborne, BRI Australia Limited, An Independent Grains Research and Development Institute, PO Box 7, North Ryde, NSW 2113, Australia

Yukihiro Ozaki, Department of Chemistry, School of Science and Technology, Kwansai-Gakuin University, 2-1, Gakuen, Sanda, 669-1337, Japan

C. Sandorfy, Departemenent de Chimie, Universite de Montreal, Montreal, Quebec, Canada H3C 377

Sirinnapa Saranwong, Nondestructive Evaluation Laboratory, Analytical Science Division, National Food Research Institute, 2-1-2, Kannondai, Tsukuba, 305-8642, Japan

Vegard H. Segtnan, MATFORSK- Norwegian Food Research Institute, Osloveien 1, N-1430 Aas, Norway

Roumiana Tsenkova, Faculty of Agriculture, Department of Environment Information and Bio-Production Engineering, Kobe University, 1-1 Rokkoudai, Nada-ku, Kobe, 657-8501, Japan

Satoru Tsuchikawa, Mechanical Engineering for Biological Materials, Biological Material Sciences, Biosphere Resources Science, Graduate School of Bioagricultural Science, Nagoya University, Furo-cho, chikusa-ku, Nagoya, 464-8602, Japan

Phil Williams, PDK Grain, Winnipeg, Manitoba, Canada

Takuo Yano, Department of Information Machine and Interfaces, Faculty of Information Sciences, Hiroshima City University, 3-4-1, Ohtsuka-Higashi, Asaminami-ku, Hiroshima, 731-3194, Japan

Introduction

W. FRED MCCLURE

WORLD FOOD PRODUCTION

The industrialized world consists of about 59 countries, all with a total populations of about 0.9 billion people, about one-sixth of the total world population. In contrast, about 5 billion people live in approximately 125 low- and middle-income countries. The remaining 0.4 billion live in countries in transition, which include the Baltic states, eastern Europe and the Commonwealth of Independent States (1). Today, our world produces food for 6.39 billion people (Fig. 1.1). Yet statistics show that many people go to bed hungry every night. Each year the food crisis intensifies and more and more people go hungry.

Shockingly, the push to produce more and more food is thwarted by diminishing arable land suitable for food production. Plant yields have been maximized for many crops, leaving few options for increasing food production. In the face of these seemingly insurmountable problems, scientists are beginning develop technology for maximizing *food potential*, a philosophy that calls on any means that will reduce waste.

The philosophy for maximizing food for fresh foods potential goes something like this.¹ Time of harvest for plant-based foods must be optimized in order to maximize food potential. If harvested too early, both yield and quality are reduced: Again, if crops left too long in the field, both yield and quality fall. Furthermore, between the time of harvest and the time of consumption fresh foods undergo a decaying process called senescence. Senescence can reduce food potential by 7–12%, depending on how

¹ “Maximizing food potential” was first introduced by W. Fred McClure at the International Conference on Planning for the Future, Newcastle University, Newcastle, UK in W. F. McClure. 1995. Biological measurements for the 21st Century. In *New Horizons, New Beginnings*, ed. Staff, 1:34–40. Newcastle University, Newcastle, UK: Newcastle University.

USA TODAY Snapshots®

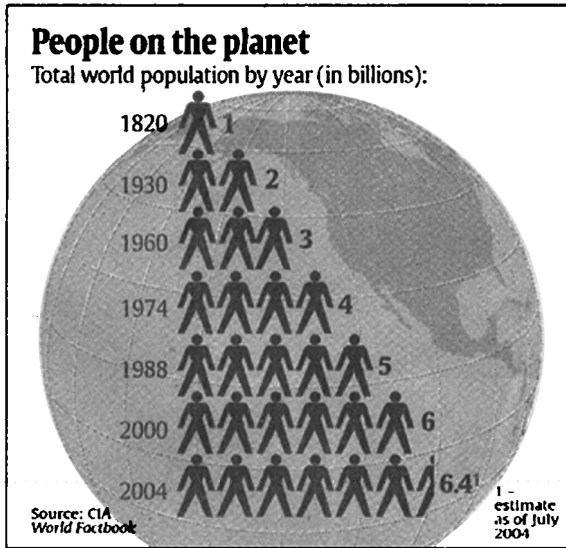


Figure 1.1. World population statistics for the USA, 1820–2004 published in CIA World Fact Book (USA Today Snapshots, July 2004).

quickly the food is made ready for consumption.² The potential exists for reducing losses if appropriate tools are made available for measuring the quality of fresh food.

Quality measurements made early in the production cycle, when fresh products are still edible, can determine whether the product goes to fresh market or to processing. The fresh market fraction with optimized quality factors is sent to fresh market; the remaining fraction is sent to facilities for further processing to make pop-tarts, jams, cooked meals and/or soups. Thus the food potential is maximized by minimizing waste.

NEAR-INFRARED SPECTROSCOPY

Near-infrared (NIR) spectroscopy has taken its place among other proven spectroscopic tools, especially for determining chemical and physical properties of foods and food products. Covering the small region of the electromagnetic spectrum from 780 to 2500 (nm) (Sheppard, 1985 #354), producing spectra with only 860 data points spaced 2 nm apart, NIR spectroscopy has experienced phenomenal growth over its short history from 1905 (the year Coblenz produced the first official NIR publication) to the

² Based on a survey taken of six major grocery chains in the USA in *Ibid.*; reported at the conference in Newcastle, UK.

TABLE 1.1. Major Constituents/Properties in Foods Determined with Near-Infrared Spectroscopy

Number	Constituent	Comment	References
1	Water	Water was the first constituent to be studied with near-infrared spectroscopy.	49
2	Protein	Williams, Norris and Kays studied of protein, oil, water and starch in pulverized wheat and foods.	10–15
3	Fats (Oils)	Fats (or oils) were in foods has become a routine NIR measurement today.	16–19
4	Cereals: Dietary Fiber	Dietary and health issues have been studied extensively.	20–23
5	Scattering Properties	Any solid material demands an understanding of the scattering properties in order to obtain robust calibrations.	24, 25
6	Sucrose	Sucrose is a critical constituent in health issues.	26
7	Carbohydrates	Dietary matters call for NIR analyses of carbohydrates.	10
8	Energy	Energy content of food determined by NIR spectroscopy	27
9	Homogeneity	Homogeneity is critical to robust calibrations.	28
10	Condiments Sucrose, Starch, Flour	Osborne has studied the combination of these constituents in processed cereals.	29
11	Meats: Beef, Poultry, Fish	Beef, poultry and fish are analyzed using NIR by a number of researchers.	30–39
12	Fresh Foods: Fruit, Nuts	Once thought to be a very difficult determination, Kawano, Saranwong and others have demonstrated that NIR is useful for the analyses of high-moisture products.	40–50
13	Honey, Corn Syrup, Molasses	Even amorphous sugars in honey and other products can be measured.	51–57
14	Candy, Chocolate, Caramel	The same is true for candies, plus the nicotine related components in chocolates.	54, 58–60

(Continued)

TABLE 1.1. (Continued)

Number	Constituent	Comment	References
15	Sweets: Sucrose, Saccharin, Honey, Corn Syrup, Molasses	The spectra of sucrose and saccharin are strikingly similar.	54, 61–65
16	Beverages: Milk, Soft and Hard	In particular, ethanol in beer, wines and spirits is easily determined with near-infrared spectroscopy.	66–78
17	Bread	Osborne has been the leader in the analysis of bread using NIR spectroscopy.	79–81

present. Its sensitivity to the CH, NH, and OH absorptions related to food components, its speedy response time, the simplicity of sample preparation involved, the fact that the measurement is nondestructive, and its low instrumentation cost have fixed its position along side other spectroscopies, including ultraviolet, visible, mid-infrared, Raman and others. Its expansion into the field of food production and processing is undeniable. (2–11)

NIR technology cuts across many fields (agriculture, textiles, pharmaceuticals, cosmetics, medicine, and others), with demonstrated success in all areas published in the literature. This book is not intended to address all the above areas. Rather, this book is intended to provide the reader an opportunity to understand something of the impact NIR spectroscopy has had on food science and technology. Expectedly, it does include basic principles of NIR spectroscopy (Chapter 2), characteristics of the NIR spectra (Chapter 3), instrumentation (Chapter 4), sampling techniques (Chapter 5), and chemometrics (Chapter 6). The remainder of the book discusses numerous applications of NIR technology in the food science field [agricultural and Marine (Chapter 7), food and food products (Chapter 8)] and some specialized applications (Chapter 9). The Editors and Authors all hope you will find this book to be helpful in your work.

REFERENCES

1. 2003 World Population Data Sheet. Population Reference Bureau. Bread for the World Institute. Accessed February 16, 2005. Electronic. Available from <http://www.bread.org/hungerbasics/international.html#cite5>.
2. G. S. Birth. *How light interacts with food*. In: *Quality Detection in Foods*, J. Gaffney, ed, 1:6–11. St. Joseph, MI, ASAE, 1976.
3. A. M. C. Davies. 1984. Progress in human food analysis by near infrared. *Anal Proc* **21**: 488–491.
4. A. M. C. Davies, A. Grant. 1987. Review: near infrared analysis of food. *Int J Food Sci Technol* **22**: 191–207.

5. G. J. DeMenna, G. J. Brown. Fast Food Analysis: Don't Wait for Proximate. *Food Testing and Analysis* (June/July): 16–19, 1998.
6. G. C. Marten, J. S. Shenk, I. F. E. Barton. 1989. *Near Infrared Reflectance Spectroscopy (NIRS): Analysis of Forage Quality (Handbook No. 643)*. Agriculture Handbook No. 643. Springfield, VA: National Technical Information Service.
7. H. Martens, H. Russwurm(Jr). *Food Research and Data Analysis*. New York, NY: Applied Science Publishers, 1983.
8. K. H. Norris. Measurement of quality in foods and agricultural commodities by physical methods. In: *First Food Physics Symposium*, 113–124, 1956.
9. B. G. Osborne, T. Fearn. *Near Infrared Spectroscopy in Food Analysis*. Essex, UK: Longman Scientific & Technical-Wiley, 1986.
10. N. S. Sahni, T. Isaksson, T. Næsby. In-line near infrared spectroscopy for use in product and process monitoring in the food industry. *J Near Infrared Spectrosc* **12**: 77–83, 2004.
11. P. Williams, K. Norris, eds, *Near-Infrared Technology in Agricultural and Food Industries (First Edition)*. St. Paul, MN: Am Assoc Cereal Chemists, 1987.

REFERENCES ON FOOD

1. E. Anklam, F. Gadani, P. Heinze, H. Pijnenburg, G. V. D. Eede. Analytical methods for detection and determination of genetically modified organisms in agricultural crops and plant-derived food products. *Eur Food Res Technol* **214**: 3–26, 2002.
2. D. D. Archibald, S. E. Kays, D. S. Himmelsbach, F. E. BARTON-II. Raman and NIR Spectroscopic Methods for Determination of Total Dietary Fiber in Cereal Foods: A Comparative Study. *Appl Spectrosc* **52(1)**: 22–31, 1998.
3. D. D. Archibald, S. E. Kays, D. S. Himmelsbach, F. E. Barton-II. Raman and NIR Spectroscopic Methods for Determination of Total Dietary Fiber in Cereal Foods: Utilizing Model Differences. *Appl Spectrosc* **52(1)**: 32–41, 1998.
4. S. Asen, R. N. Stewart, K. H. Norris. A naturally occurring colorant for food and beverages. U. S. Department of Commerce, 1978.
5. D. Baker. The determination of fiber in processed cereal foods by near infrared reflectance spectroscopy. *Cereal Chemistry* **60**: 217–219, 1983.
6. D. Baker, K. H. Norris, B. W. Li. *Food fiber analysis: Advances in methodology*. In: *Dietary Fibers: Chemistry and Nutrition*, A. Inglett, S. I. Falkehag, eds, 68–78. New York: Academic Press, 1979.
7. R. J. Barnes, M. S. Dhanoa, S. J. Lister. Correction to the description of Standard Normal Variate (SNV) and De-Trend (DT) transformations in Practical Spectroscopy with Applications in Food and Beverage Analysis—2nd Edition. *J Near Infrared Spectrosc* **1(2)**: 185–186, 1993.
8. E. O. Beasley. Light transmittance of peanut oil as an objective measurement related to quality of raw peanuts. In: *Quality Detection in Foods*, J. J. Gaffney, ed, **1**: 50–52. St. Joseph, MI: American Society of Agricultural Engineers, 1976.
9. G. S. Birth. *How light interacts with food*. ASAE Paper.
10. G. S. Birth. *Research in food instrumentation*. Instrument Society of America, 1963.

11. G. S. Birth. How light interacts with foods. In: *Quality Detection in Foods*, J. J. Gaffney, ed, **1**: 6–11. St. Joseph, MI: American Society of Agricultural Engineers, 1976.
12. G. S. Birth. The light scattering properties of food. *J Food Sci* **43**: 916–925, 1978.
13. G. S. Birth. Radiometric measurement of food quality—a review. *J Food Sci* **44**: 949–953, 957, 1979.
14. G. S. Birth, K. H. Norris. The difference meter for measuring interior quality of foods and pigments in biological tissues. Technical Bulletin No. 1341: 19-Jan, 1965.
15. G. S. Birth, K. L. Norris. The difference meter an instrument for measuring interior quality of foods. Asae, 1963.
16. O.-C. Bjarno. Meat and meat products: Multicomponent analysis of meat products. *J Assoc Off Anal Chem* **64(6)**: 1392–1396, 1981.
17. O.-C. Bjarno. Multicomponent analysis of meat products by infrared spectrophotometry: Collaborative Study. *J Assoc Off Anal Chem* **65(3)**: 696–700, 1982.
18. M. M. Brown, I. J. Ross. The use of radio frequency fields as a means of determining the concentration and volume of solutions of food components. Asae, 1967.
19. A. Brynjolfsson. The national food irradiation program conducted by the department of the army.
20. H. Buning-Pfaue. Analysis of water in food by near infrared spectroscopy. *Food Chemistry* **82**: 107–115, 2003.
21. C. S. Burks, F. E. Dowell, F. Xie. Measuring fig quality using near-infrared spectroscopy. In: Preprint, 2000.
22. D. J. Casimir, Countercurrent extraction of soluble solids from foods. *Csiro Fd Res Q* **43**: 38–43, 1983.
23. P. Chandley. The application of the DESIR technique to the analysis of beer. *J Near Infrared Spectrosc* **1(1)**: 133–139, 1993.
24. J. Y. Chen, C. Iyo, S. Kawano, F. Terada. Development of calibration with sample cell compensation for determining fat content in unhomogenized raw milk by a simple NIR transmittance method. *J Near Infrared Spectrosc* **7**: 265–273, 1999.
25. A. M. C. Davies, J. Franklin, K. M. Wright, S. M. Ring, P. S. Belton. FT – the solution to many problems. Laboratory Practice Preprint, 1985.
26. G. J. DeMenna, G. J. Brown. Fast Food Analysis: Don't Wait for Proximate. *Food Testing and Analysis (June/July)*: 16–19, 1998.
27. E. Díaz-Carrillo, A. Muñoz-Serrano, A. Alonso-Moraga, J. M. Serradilla-Manrique. Near infrared calibrations for goat's milk components: protein, total casein, as-, b- and k-caseins, fat and lactose. *J Near Infrared Spectrosc* **1(2)**: 141–146, 1993.
28. M. R. Ellekjær, K. I. Hildrum, T. Næs, T. Isaksson. Determination of the sodium chloride content of sausages by near infrared spectroscopy. *J Near Infrared Spectrosc* **1**: 65–75, 1993.
29. D. G. Evans, C. N. G. Scotter, L. Z. Day, M. N. Hall. Determination of the authenticity of orange juice by discriminant analysis of near infrared spectra: A study of pretreatment and transformation of spectral data. *J Near Infrared Spectrosc* **1(1)**: 33–44, 1993.
30. P.-G. Fyhn, E. Slinde. Measurements of monochromatic visible light changes within food products using laser and fiber optics. *Norwegian Food Research Institute* 11-Jan, 1985.
31. T. Gato. Application of near-infrared spectroscopy for predicting the moisture, total nitrogen and neutral density fiber of raw tea and tea. In: *2nd International NIRS*

- Conference, M. Iwamoto, S. Kawano, eds, 319–328. Tsukuba, Japan: Korin Publishing Co., 1989.
32. T. Goto. Application of near infrared spectroscopy for predicting the moisture, total nitrogen and neutral detergent fiber of raw tea and tea. *Proc 2nd Intl NIRS Conf, Tsukuba, Japan* **1**: 319–328, 1989.
 33. H. Abe, S. Kawano, K. Takehara, M. Iwamoto. Determination of Sucrose content in Sugarcane Juice by Near Infrared Spectroscopy, *Rep Natl Food Res Inst* **60**: 31–36. Tsukuba, Japan: Food Research Institute, 1996.
 34. T. Hagiwara, H. Wang, T. Suzuki, R. Takai. Fractal Analysis of Ice Crystals in Frozen Food. *J Agric Food Chem* **50**: 3085–3089, 2002.
 35. A. J. Hand, D. C. McCarthy. Interactive story: From corn to cupcakes. *Photonics Spectra* **34(3)**: 91–103, 1999.
 36. A. J. Hand, D. C. McCarthy. Photonics and Food. *Photonics Spectra* **34(3)**: 89–124, 1999.
 37. K. Ikegaya, M. Iwamoto, J. Uozumi, R. K. Cho. Determination of chemical composition of Japanese green tea by near-infrared spectroscopy. M. Iwamoto, S. Kawano, eds, *2nd International NIRS Conference. Tsukuba, Japan*: Korin Publishing Co., 1990.
 38. K. Ikegaya, S. Kawano, R. K. Cho. Determination of theaflavins in black tea by near-infrared spectroscopy. In: *2nd International NIRS Conference*, M. Iwamoto, S. Kawano, eds, Tsukuba, Japan: Korin Publishing, 358, 1989.
 39. T. Isaksson, Z. Wang, B. Kowalski. Optimised scaling (OS-2) regression applied to near infrared diffuse spectroscopy data from food products. *J Near Infrared Spectrosc* **1**: 85–97, 1993.
 40. K. J. Kaffka, J. Farkas, Z. Seregely, L. Meszaros. Monitoring the effect of ultra-high pressure preservation technology by near infrared reflectance spectroscopy. In: *Near Infrared Spectroscopy: Proceedings of the 10th International Conference*, A. M. C. Davies, R. K. Cho, eds, Preprint: 505. Kyongju, Korea: NIR Publication, UK, 2002.
 41. S. Kawano, H. Abe, M. Iwamoto. Development of a calibration equation with temperature compensation for determining the Brix value in intact peaches. *J Near Infrared Spectrosc* **3**: 211–218, 1995.
 42. S. E. Kays. The use of near infrared reflectance spectroscopy to predict the insoluble dietary fibre fraction of cereal products. *J Near Infrared Spectroscopy* **6**: 221–227, 1998.
 43. S. E. Kays, F. E. Barton-II. Near-Infrared Analysis of Soluble and Insoluble Dietary Fiber Fractions of Cereal Food Products. *J Agric Food Chem* **50**: 3024–3029, 2002.
 44. S. E. Kays, F. E. Barton-II. Rapid Prediction of Gross Energy and Utilizable Energy in Cereal Food Products Using Near-Infrared Reflectance Spectroscopy. *J Agric Food Chem* **50**: 1284–1289, 2003.
 45. S. E. Kays, F. E. Barton-II, W.R. Windham. Predicting protein content by near infrared reflectance spectroscopy in diverse cereal food products. *J Near Infrared Spectrosc* **8**: 35–43, 2000.
 46. G. Kisko, Z. Sertegely. Qualification of volatile oils using NIR and electronic nose. In: *10th International Conference on Near Infrared Spectroscopy (KOREA)*, A. M. C. Davies, ed, Preprint: 12. Kyongju, Korea: NIR Publication, UK, 2001.
 47. I. M. E. Lafargue, M. H. Feinberg, J.-J. Daudin, D. N. Rutledge. Homogeneity check of agricultural and food industries samples using near infrared spectroscopy. *Anal Bioanal Chem* **375**: 496–904, 2003.

48. I. Landa. Food constituents analysis using a monochromator with high speed scan and high energy throughput. In: *Meeting of the ASAE:17*. Winnipeg, Canada: ASAE, 1979.
49. H. Martens. Understanding food research data. *Applied Science*: May 38, 1982.
50. H. Martens, H. Russwurm(Jr). *Food Research and Data Analysis*. New York, NY: Applied Science Publishers, 1983.
51. K. A. Martin. Recent advances in near-infrared reflectance spectroscopy. In: *Applied Spectroscopy Reviews*, Jr. Edward, G. Brame, eds, **27**: 325–383. New York, NY: Marcel Dekker, Inc., 1992.
52. D. R. Massie. A high-intensity spectrophotometer interfaced with a computer for food quality measurement. In: *Quality Detection in Foods*, J. J. Gaffney, ed, **1**: 12–15. St. Joseph, MI: American Society of Agricultural Engineers, 1976.
53. D. C. McCarthy. The perfect chocolate chip cookie. *Photonics Spectra* **34(3)**: 105–111, 1999.
54. D. C. McCarthy. The perfect orange. *Photonics Spectra* **34(3)**: 113–117, 1999.
55. D. C. McCarthy. Vision shouldn't blur your beer. *Photonics Spectra* **34(3)**: 119–124, 1999.
56. W. F. McClure. Biological measurements for the 21st century: Instruments – First; Measurements – Second; Discovery – Third. In: *Agricultural and Biological Engineering: New Horizons, New Challenges*, Miron Turner, ed, 1–9. Newcastle, UK: Tynesoft Business Services, 1995.
57. W. F. McClure. Wave of the future: *Biomeasurements in the 21st Century*. Conference Talk, 1995.
58. W. F. McClure. Near-infrared Instrumentation. In: *Near-Infrared Technology in the Agricultural and Food Industries, Second Edition*, Phil Williams, Karl Norris, eds, 109–127. St. Paul, MN: American Association of Cereal Chemists, 2001.
59. S. C. Mohapatra. *World Hunger. Resource* **4 (April)**: 33, 1999.
60. N. N. Mohsenin. Application of mechanical properties of food materials in quality evaluation and control. *Asae Paper No. 73–6510*, 1973.
61. I. Murray. Nir Analysis- How Near Infrared Reflects Composition. In: *One Day Seminar on the Use of Near Infrared Reflectance (NIR) Analysis in Research, Routine and Run-Of-The-Mill Applications*, **1**: 51, School of Agriculture, Aberdeen, Scotland: Chemistry Division, School of Agriculture, 1983.
62. W. W. News. High pressure touted as improved method of food preservation, 1998.
63. S. L. Oh, R. K. Cho, B. Y. Min, D. H. Chung, S. Kawano, K. Ikegaya. Determination of nitrogen compounds in green tea infusion by near-infrared reflectance spectroscopy. In: *2nd International NIRS Conference*, M. Iwamoto, S. Kawano, eds, 376–385. Tsukuba, Japan: Korin Publishing, 1990.
64. T. P. Ojha, A. W. Farrall, A. M. Dhanak, C. M. Stine. Determination of heat transfer through powdered food products. *Asae*, 1966.
65. B. G. Osborne. Near infrared spectroscopic studies of starch and water in some processed cereal foods. *J Near Infrared Spectrosc* **4**: 195–200, 1996.
66. B. G. Osborne, T. Fearn. *Near Infrared Spectroscopy in Food Analysis*. Essex, UK: Longman Scientific & Technical-Wiley, 1986.
67. N. Pedretti, D. Bertrand, M. Semenou, P. Robert and R. Giangiacomo. Application of an experimental design to the detection of foreign substances in milk. *J Near Infrared Spectrosc* **1(2)**: 174–184, 1993.

68. O. Pelletier, R. Brassard. Determination of vitamin c (l-ascorbic acid and dehydroascorbic acid) in food by manual and automated photometric methods. Bureau of Nutritional Sciences, Ottawa, Canada: 1–11, 1983.
69. D. D. Requena, S. A. Hale, D. P. Green, W. F. McClure, B. E. Farkas. Detection of discoloration in thermally processed blue crab meat. *Journal of the Science of Food and Agriculture* **79**: 786–791, 1999.
70. P. Robert, M. F. Devaux, A. Qannar, M. Safara. Mid and near infrared study of carbohydrates by canonical correlation analysis. *J Near Infrared Spectrosc* **1**: 99–108, 1993.
71. L. E. Rodriguez-Saona, F. S. Fry, E. M. Calvey. Use of Fourier Transform Near-Infrared Reflectance Spectroscopy for Rapid Quantification of Castor Bean Meal in a Selection of Flour-Based Products. *J Agric Food Chem* **48**: 5169–5177, 2000.
72. J. M. Roger, V. Bellon-Maurel. Improving sugar content prediction in fruits by applying genetic algorithms to near infrared spectra. *J NIRS* (Preprint for Review): 1–29, 1999.
73. S. Sasic, Y. Ozaki. Wavelength-wavelength and sample-sample two dimensional correlation analyses of short-wave near-infrared spectra of raw milk. *Appl Spectrosc* Preprint for Review, 2000.
74. V. H. Segtnan, T. Isaksson. Evaluating near infrared techniques for quantitative analysis of carbohydrates in fruit juice model systems. *JNIRS* **8**: 108–116, 2000.
75. Z. Seregely, K. J. Kaffka. Qualification of food flavors using NIR spectroscopy and chemosensor-array (electronic nose). *JNIRS* Preprint for Review: 1–7, 2001.
76. S. K. Seymour, D. D. Hamann. Design of a microcomputer-based instrument for crispness evaluation of food products. In: *Meeting of the ASAE*.
77. S. K. Seymour, D. D. Hamann. Design of a microcomputer-based instruments for crispness evaluation of food products. *Transactions of the ASAE* **27(4)**: 1245–1250, 1984.
78. O. P. Snyder. Food radiation, *the process engineering challenge*. Asae, 1966.
79. Staff. *NIR Analysis: How Near Infrared Reflects Composition*. Aberdeen, Scotland, 1983.
80. A. S. Szabo, P. Tolnay, Z. Mednyanszky. Monitoring changes in material properties of agricultural products during heating and drying by impedance spectroscopic analysis. *1st Intl Conf on Food Physics* **1**: 96–98, 1994.
81. T. Takeo, N. Okamoto. Quality control of tea by near-infrared reflectance spectroscopy. In: *2nd International NIRS Conference*, M. Iwamoto, S. Kawano, eds, 157–173. Tsukuba, Japan: Korin Publishing Co., 1989.
82. D. P. Thompson, J. C. Wolf. Available lysine losses in a stirred model food system. American Society of Agricultural Engineers, 1976.
83. K. Thyholt, T. Issaksson. Near infrared spectroscopy of dry extracts from high moisture food products on solid support: A review. Preprint, 1998.
84. U. Wahlby, C. Skjoldebrand. NIR-measurements of moisture change in foods. *J Food Engineering* **47**: 303–312, 2001.
85. B. Welz, Z. Grobanski, M. Melcher, D. Weber. *A techniques in food analysis*. Atomic Absorption Perkin Elmer Corp, 1979.
86. D. L. B. Wetzel. Analytical near infrared spectroscopy. (In: *NIR near infrared food beverage instrumentation chemometrics* (D. Wetzel, G. Charalambous, eds, Elsevier Science B. V., New York. Book: 141–194, 1998.
87. P. Williams, K. Norris. Eds, *Near-Infrared Technology in Agricultural and Food Industries (First Edition)*. St. Paul, MN: Am Assoc. Cereal Chemists, 1987.

88. P. Williams, K. Norris. Eds, *Near-Infrared Technology in Agricultural and Food Industries (Second Edition)*. St. Paul, MN: Am Assoc. Cereal Chemists, 2001.
89. R. H. Wilson. Ed, *Spectroscopic Techniques for Food Analysis (COPY of book ON SHELF)*. Edited by n/a. n/a. New York, NY: VCH Publishers, Inc., 1994.
90. J. P. Wold. Rapid quality assessment of meat and fish by using near-infrared spectroscopy, autofluorescence spectroscopy and image analysis. Doctor of Science, Agricultural University of Norway, 2000.
91. R. Yabe. Near-infrared transmittance application for determining moisture content of surimi products. In: *Proc 2nd Intl NIRS Conf, Tsukuba, Japan:190–195*, 1989.
92. H. Yang, J. Irudayaraj. Rapid determination of vitamin C by NIR, MIR and FT-Raman techniques. *J Pharmacy and Pharmacology* **54**: 1–7, 2002.
93. X. Zhao, W. Chan, M. Wong, D. Xiao, Z. Li. A fluorescence-based iodine sensor for food analysis. *Am Laboratory* **35(11)**: 13–21, 2003.

Principles of Molecular Vibrations for Near-Infrared Spectroscopy

C. SANDORFY, R. BUCHET, and G. LACHENAL

INTRODUCTION

The fundamental vibrations of molecules lead to absorption in the infrared (200–4000 cm^{-1}), while their overtones and combination tones appear in the infrared and in the near infrared. The highest wavenumber associated to an infrared active fundamental vibration appears at 3998 cm^{-1} for HF; therefore 4000 cm^{-1} is somehow the border of the infrared and the near infrared. The near-infrared spectrum is located between the infrared and the visible, from 2500 nm to 800 nm or from 4000 cm^{-1} to 12,500 cm^{-1} . It is sometimes called the overtone region, but, naturally, the first overtone of vibrations of lower wavenumber are in the mid-infrared. As a rule overtones and combination tones are much weaker than the fundamentals, the first ones usually by a factor of 10 to 100. Second and higher overtones and combination tones are even weaker. The near-infrared absorption of polymers, especially in the region from 4000 to 9000 cm^{-1} , originates from the overtones of OH, NH, CH, and SH stretching vibrations as well as from stretching-bending combinations involving these groups. The overtones and combination tones are most often affected by hydrogen bond formation, certain aspects of which can be monitored to advantage in the near infrared (1). In addition, a few electronic transitions may appear in the upper range of the near infrared, close to the visible, especially in the range of 9000 cm^{-1} to 15,000 cm^{-1} . For example, electronic transitions of oxyhemoglobin and deoxyhemoglobin give rise to a band around 13,160 cm^{-1} (760 nm). Because most of the analytical applications of near-infrared spectroscopy on polymers and biomolecules are centered in the 4000- cm^{-1} to 9000- cm^{-1} region, the present review focuses on overtones and combination tones of molecular vibrations.

Two languages are available for the treatment of overtones: the language based on normal coordinates (2–5) and the more recent treatment based on local coordinates (6–9). Whereas the latter appears to be better adapted to higher overtones, especially when kinetics of chemical reactions are concerned, the first overtones are treated well on a normal coordinate basis. In what follows, normal coordinates will be used; then we discuss the approach based on local coordinates.

THE DIATOMIC OSCILLATOR

The simplest possible assumption about the form of the vibrations in a diatomic molecule is that each atom moves toward or away from the other in a simple harmonic motion (2–5). Such a motion of the two atoms can be reduced to the harmonic vibration of a single mass point about an equilibrium position. In classic mechanics a harmonic oscillator can be defined as a mass point of mass m that is acted upon by a force F proportional to the distance Q from the equilibrium position and directed toward the equilibrium position:

$$F = m \frac{\partial^2 Q}{\partial t^2} = -kQ \quad (2.1)$$

where the proportionality factor k is called the force constant and depends only on the strength of the chemical bond. The solution of the differential equation is:

$$Q = Q_0 \sin(2\pi \nu t + \phi) \quad (2.2)$$

Q_0 is the amplitude of the vibration, ϕ is a phase constant dependent on the initial conditions, and ν is the vibrational frequency. The displacement of the point mass from the equilibrium position is a sine function of time. By substituting Equation 2.2 into Equation 2.1, it follows that:

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{m}} \quad (2.3)$$

Because the force is the negative derivative of the potential energy U , using Equation 2.1 one obtains that:

$$U = \frac{1}{2}kQ^2 = 2\pi^2 m \nu^2 Q^2 \quad (2.4)$$

The potential energy of a harmonic oscillator is proportional to the square of the displacement from the equilibrium position. The restoring force exerted by the two atoms of a molecule on each other when they are displaced from their equilibrium position (r_e) is approximately proportional to the change of internuclear distance

$(r - r_e)$. For the first atom, of mass m_1 :

$$m_1 \frac{\partial^2 r_1}{\partial t^2} = -k(r - r_e) \quad (2.5)$$

For the second atom of mass m_2 :

$$m_2 \frac{\partial^2 r_2}{\partial t^2} = -k(r - r_e) \quad (2.6)$$

where $Q = (r - r_e)$ is the displacement from the equilibrium position, r_1 and r_2 are the distance of the two atoms from the center of gravity, r is the distance of the two atoms from each other, and r_e is the equilibrium distance. For a dumbbell model of a diatomic molecule:

$$r_1 = \frac{m_2}{m_1 + m_2} r \quad \text{and} \quad r_2 = \frac{m_1}{m_1 + m_2} r \quad (2.7)$$

By substituting Equation 2.7 into either Equation 2.5 or Equation 2.6 one can obtain:

$$f = \frac{m_1 m_2}{m_1 + m_2} \frac{\partial^2 Q}{\partial t^2} = -kQ \quad (2.8)$$

$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$

μ is so-called reduced mass.

Equation 2.8 is identical to Equation 2.1 of the harmonic oscillator, except that Q is replaced by $Q = (r - r_e)$. The vibration of the two atoms of a molecule is reduced to the vibration of a single mass point of mass μ . From Equation 2.8 it follows that:

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} \quad (2.9)$$

Usually, the wavenumber ($\bar{\nu}$) is used in infrared and near-infrared spectroscopy. Equation 2.9 is often written as:

$$\bar{\nu} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} \quad (2.10)$$

The frequency of the vibrational mode depends on two parameters: the reduced mass μ and the force constant k . It follows from this equation that isotopic labeling is a powerful tool to assign bands in infrared and near-infrared spectra. For example, the CH_2 symmetric stretching of lipid is located at 2851 cm^{-1} , whereas the C^2H_2 symmetric stretching of perdeuterated lipid is at 2070 cm^{-1} (10). Assuming that k

is not affected during the isotopic substitution and assuming that CH_2 and C^2H_2 symmetric stretching modes behave like vibrational modes of a diatomic molecule, by using Equation 2.10 and computing the reduced mass of CH and of C^2H , the theoretical ratio of the two wavenumbers $\bar{\nu}(\text{CH})/\bar{\nu}(\text{C}^2\text{H})$ can be obtained:

$$\mu(\text{CH}) = \frac{12 \times 1}{12 + 1} = 0.923$$

$$\mu(\text{C}^2\text{H}) = \frac{12 \times 2}{12 + 2} = 1.714$$

$$\bar{\nu}(\text{CH})/\bar{\nu}(\text{C}^2\text{H}) = (\mu(\text{C}^2\text{H})/\mu(\text{CH}))^{1/2} = 1.36$$

For comparison, the ratio of the two measured wavenumbers is $2851/2070 = 1.38$. Although the lipid is not a diatomic molecule, the CH vibrational mode behaves almost like a diatomic molecule. Some vibrational modes in polymers that are very well localized can be considered as vibrational modes of a diatomic molecule. Fortunately, most of the first overtones and combination tones in the near infrared arise from well-localized vibrational modes such as OH, NH, CH, and SH stretching modes. The force constant k depends on the strength of the chemical bond, which is mainly controlled by the electronic environment surrounding atoms in molecules. Electrostatic interactions or formation of hydrogen bonds alter the force constant k and therefore can shift the frequency. It is well established that infrared and near-infrared spectroscopies are very sensitive in detecting the formation of hydrogen bonds. For example, a change in hydrogen bonding distance of only 0.0002 nm shifts the wavenumber of the stretching vibration of NH of a peptide backbone by approximately 1 cm^{-1} . This shift is well within the experimental limit. In contrast, X-ray crystallographic results rarely have a resolution below 0.1 nm (11). Classically, only one vibrational frequency is possible according to Equation 2.9, whereas its amplitude and its energy can assume any value.

ENERGY LEVELS

In quantum mechanics, the vibration in a diatomic molecule may also be reduced to the motion of a single point mass of mass μ , whose displacement Q from its equilibrium position corresponds to $(r - r_e)$. Assuming that the potential is that of a one-dimensional harmonic oscillator (4), the Hamiltonian H becomes:

$$H = \frac{h^2}{8\pi^2\mu} \frac{\partial^2}{\partial Q^2} + \frac{1}{2}kQ^2 \quad (2.11)$$

Using the Schrödinger equation:

$$\left(\frac{h^2}{8\pi^2\mu} \frac{\partial^2}{\partial Q^2} + \frac{1}{2}kQ^2 \right) \psi(Q) = E\psi(Q) \quad (2.12)$$

The Hermite polynomials are the wavefunctions that satisfy Equation 2.12. For a diatomic molecule the Hermite polynomials have the form (5):

$$\psi_v = N_v e^{\frac{1}{2}Q^2} H_v(\sqrt{\alpha}Q) \quad (2.13)$$

where $\alpha = \frac{4\pi^2}{h} \mu \nu = \frac{2\pi}{h} \sqrt{\mu k}$, μ is the reduced mass, h is the Planck constant, k is the harmonic potential constant, and N_v is the normalization factor. Then for successive values of the vibrational quantum number v we have with $\sqrt{\alpha}Q = z$

$$H_0(z) = 1$$

$$H_1(z) = 2z$$

$$H_2(z) = 4z^2 - 2$$

$$H_3(z) = 8z^3 - 12z$$

$$H_4(z) = 16z^4 - 48z^2 + 12$$

$$H_5(z) = 32z^5 - 160z^3 + 120z$$

The solution of Equation 2.12 indicates that the vibrational energies $E(v)$ have discrete values (4).

$$E(v) = \left(v + \frac{1}{2}\right) \frac{h}{2\pi} \sqrt{\frac{k}{\mu}} \quad (2.14)$$

$$E(v) = \left(v + \frac{1}{2}\right) h\nu \quad (2.15)$$

where the vibrational quantum number v can take only integral values, 0, 1, 2, ... These values are the only energy values allowed by theory for the harmonic oscillator. ν is the vibrational frequency of the diatomic molecule as defined in Equation 2.9. The lowest energy ($v = 0$) has $E(0) = (1/2)h\nu$. Thus even in the lowest state, the vibrational energy of a molecule is not zero, in contrast to the result of classic mechanics. Equation 2.14 is often written in wavenumber units as:

$$G_v = \frac{E(v)}{hc} = \left(v + \frac{1}{2}\right) \omega_e \quad (2.16)$$

SELECTION RULES

If the diatomic molecule in its equilibrium position has a dipole moment as in heteronuclear diatomic molecules, it will in general change if the internuclear distance varies. To a first approximation it may be assumed that the change of dipole moment with internuclear distance is linear. Therefore the dipole moment changes with a frequency equal to the frequency of the mechanical vibration. On the basis of classic

electrodynamics, this would lead to the emission of light of frequency ν . Conversely, the oscillator could be set in vibration by absorption of light of frequency ν . In quantum mechanics, emission of radiation takes place as a result of a transition of the oscillator from a higher to a lower state, and absorption is the reverse process (2). The wave number of the emitted or absorbed light is given by:

$$\nu^{v'v''} = \frac{E(v')}{hc} - \frac{E(v'')}{hc} \quad (2.17)$$

where v' and v'' are vibrational quantum numbers of the upper and the lower states, respectively. To determine which particular transitions can occur, the transition moment that corresponds to the probability of the transition from an initial to a final state must be evaluated. The transition moment for a vibrational transition is given by (2-5, 12):

$$R^{v'v''} = \int \psi_{v'}^* M \psi_{v''} \partial \tau \quad (2.18)$$

where $\psi_{v'}$ and $\psi_{v''}$ are the vibrational wave functions for the upper and lower vibrational states with their respective quantum numbers v' and v'' and M is the variable dipole moment. The well-known selection rule is $\Delta v = \pm 1$, that is, only quantum jumps by 1 are allowed. Therefore fundamental vibrations are allowed while overtones are not. This selection rule is based on the properties of the harmonic oscillator wave functions that are the normalized Hermite polynomials (Equation 2.13). Thus it only applies to the harmonic oscillator that is ruled by a quadratic potential, that is, as long as the wave functions are the exact Hermite polynomials. These conditions are never exactly met; overtones and combination bands do appear in the spectra. It is instructive to remember how this selection rule is obtained. The variable dipole moment is, if we neglect higher terms:

$$M = M_e + M_1 Q = M_e + \left(\frac{\partial M}{\partial Q} \right)_e Q \quad (2.19)$$

where $\left(\frac{\partial M}{\partial Q} \right)_e$ is taken at the equilibrium geometry. So the transition moment becomes:

$$R^{v'v''} = M_e \int \psi_{v'}^* \psi_{v''} \partial Q + \left(\frac{\partial M}{\partial Q} \right)_e \int \psi_{v'}^* Q \psi_{v''} \partial Q \quad (2.20)$$

The first term is zero because of the orthogonality of the harmonic oscillator wave functions, and the integral in the second term is, because $\partial z = \sqrt{\alpha} \partial Q$:

$$\int \psi_{v'}^* Q \psi_{v''} \partial Q = \frac{N_{v'} N_{v''}}{\alpha} \int H_{v'}(z) z H_{v''}(z) e^{-z^2} \partial z \quad (2.21)$$